

Engineered zero-dispersion microcombs using CMOS-ready photonics

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Normal group velocity dispersion (GVD) microcombs offer high comb line power and high pumping efficiency compared to bright pulse microcombs. The recent demonstration of normal GVD microcombs using CMOS foundry-produced microresonators is an important step toward scalable production. However, the chromatic dispersion of CMOS devices is large and impairs the generation of broadband microcombs. Here, we report the development of a microresonator in which GVD is reduced due to a coupled-ring resonator configuration. Operating in the turnkey self-injection locking mode, the resonator is integrated in a hybrid manner with a semiconductor laser pump to produce high-power efficiency combs spanning a bandwidth of 9.9 nm (1.22 THz) centered at 1560 nm, corresponding to 62 comb lines. Fast, linear optical sampling of the comb waveform is used to observe the rich set of near-zero GVD comb behaviors, including soliton molecules, switching waves (platicons), and their hybrids. Tuning of the 20 GHz repetition rate by electrical actuation enables servo locking to a microwave reference, which simultaneously stabilizes the comb repetition rate, offset frequency, and temporal waveform. This integrated hybrid system could be used in coherent communications or for ultrastable microwave signal generation by two-point optical frequency division. © 2023 Optica Publishing Group under the terms of the [Optica Open Access Publishing Agreement](https://doi.org/10.1364/OPTICA.478710)

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1. INTRODUCTION

Soliton mode locking in optical microresonators [1] is receiving intense interest for chip-scale integration of frequency comb systems [2–4]. An important advancement has been the realization of microcombs that are directly pumped by semiconductor lasers without amplification [5–8]. These systems are the result of steady progress in boosting the resonator Q factor to lower the pumping power, especially in detectable-rate microcombs [7,9–14]. The directly pumped systems benefit from self-injection locking (SIL) of the pump by feedback from the microcomb resonator [15,16]. SIL operation simplifies integration by eliminating the optical isolator component between the pump and the microcomb, and it also narrows the pump line. Critically, it has also been shown that SIL tends to simplify the soliton turn-on process, making it deterministic (or turnkey) for bright solitons [6].

Normal GVD dispersion microcombs [17] have also been shown to benefit from SIL operation [7,18,19]. Not only does the pulse triggering become deterministic, but the switching-wave stability dynamics that normally favor large or very small duty cycles, are overcome and the pulse duty cycle lies closer to the ideal

50% for maximal comb power and efficiency [18]. This is advantageous for microwave generation as well as for use of the microcomb as a WDM communications source [20]. Despite these useful properties of the normal GVD SIL microcombs, the spectral width of these systems is limited. For example, in high- Q CMOS-ready resonators, comb lines extend to about 4 nm due to the strong normal chromatic dispersion of the low-confinement waveguides [7,21]. An intriguing approach to extend bandwidth has been to drive microcombs near the zero GVD wavelength where pulse formation is influenced by higher-order dispersion [22–24]. In addition to permitting a range of new pulse behaviors as the system is operated above, below, or near the zero-dispersion wavelength, flattening in the dispersion spectrum is generally possible, which broadens the comb span. Under pulsed pumped operation near octave span detectable repetition rates have been possible [22].

Here, dual coupled-ring (CR) resonators are used to produce near-zero GVD microcombs using the normal dispersion CMOS-ready platform. While prior zero-GVD systems have used pulse pumping or optical amplification of CW sources, the CR resonators feature high intrinsic Q factors over 100 million (the

highest of any CR resonator system), enabling SIL operation of the microcombs with a heterogeneously integrated III-V laser. This is also, to the best of our knowledge, the first application of the SIL mode of operation to zero-GVD on-chip systems. This application provides the turnkey benefit previously observed for anomalous and normal dispersion systems, including a high efficiency comb operation [18]. Comb bandwidth up to 9.9 nm (1.22 THz) is set by design for application in a two-point optical frequency division system [25,26]. This significantly improves upon prior CMOS-ready designs and also offers the high comb line powers required in the division system. The number of comb lines generated is large for nonamplified and non-pulse-pumped zero-GVD systems. The precise stepper-lithography-defined geometry of the CMOS-ready system also enables good control of the zero-GVD wavelength. By tuning the pumping laser near the zero-dispersion point, various mode-locked comb states at microwave rates are observed. In addition, by using the linear optical sampling technique assisted by an electro-optic frequency comb [27], the temporal profiles of these states are measured including soliton molecules [22,23], switching waves [18,19], and their hybrids [22]. Numerical modeling is in agreement with the optical spectra as well as the measured temporal profiles. Servo locking of the microcomb repetition rate to a microwave reference is also demonstrated and is observed to stabilize the offset frequency and temporal waveform.

2. HIGH-Q CMOS COUPLED-RING SYSTEM

In the experiment, high- Q silicon nitride (SiN) coupled rings are fabricated using the CMOS-ready process [7], as shown in Fig. 1(a). The silicon nitride layer thickness is chosen as 100 nm to maintain single mode propagation while also boosting the Q factor [7]. Intrinsic Q factors over 100 million are achieved, as discussed in Supplement 1. The resonators are overcoupled with two bus waveguides, shown in Figs. 1(a) and 1(b) to enhance the comb efficiency (loaded Q factor is 26 million). The uncoupled resonators feature normal dispersion and will generate dark pulse combs when operated in the SIL configuration. Strong resonator coupling

is introduced to lower the dispersion, creating two zero GVD wavelengths (around 1542 and 1559 nm), as shown in Fig. 1(c). A discussion on repeatability of dispersion between different devices is included in Supplement 1, Note 5.

CR resonators [28] offer a convenient way to engineer anomalous dispersion into systems comprised of normal dispersion waveguides [29,30]. Recently, they have been studied in the context of normal GVD solitons to engineer either zero-GVD [22] or controlled (as opposed to accidentally avoided [17]) mode crossing through hybridization of a single mode pair in a photonic molecule [31]. Here, this hybridization is engineered to be broadband to spectrally flatten the dispersion curve and make higher-order dispersion important. This is done in two ways: First, the strong mutual coupling of rings is introduced, where nearly 40% of the mode power is coupled between resonators; and second, the ring free-spectral range (FSR) values are closely matched (the FSR difference is 100 MHz on FSRs close to 20 GHz). The Q factors of the coupled rings are also much higher, enabling both detectable-rate comb operation and hybrid integration with a III-V pump.

3. DISPERSION AND SIL MICROCOMB SPECTRA

In the measurement, a DFB laser operating in the vicinity of one of the two zero-dispersion wavelengths is butt-coupled to the resonator with ~ 30 – 40 mW power coupled onto the waveguide, as shown in Figs. 1(a) and 1(b). Rayleigh scattering inside the resonator reflects $\sim 2\%$ of the power into the pumping laser. An Emcore DFB laser is used to pump near 1559 nm and a PhotonX DFB laser is used to pump near 1541 nm. Microcomb optical spectra for pumping near these wavelengths are shown in Fig. 1(d). Typical microwave spectra of detected comb light are presented in Fig. 1(e) and Fig. 1(f). Temperature tuning of the DFB lasers allows fine tuning control of the pumping wavelength for access to slightly anomalous, near-zero, and slightly normal dispersion wavelengths of the resonator. Figure 2(a) shows measurements of integrated dispersion of the resonator for pumping at specific wavelengths

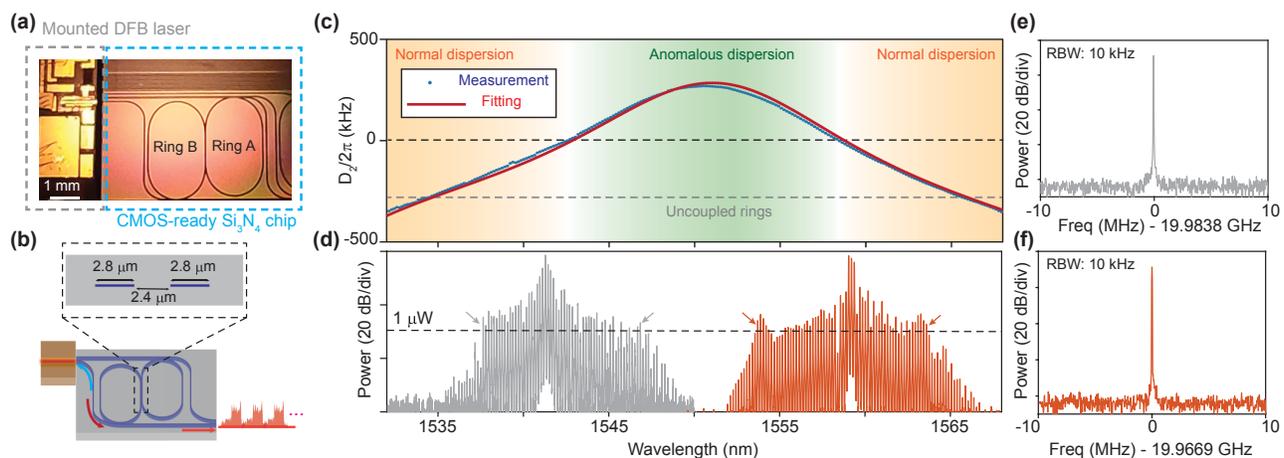


Fig. 1. Self-injection locked zero-dispersion microcomb using a CR resonator. (a) CR resonators showing DFB pump laser. The two rings feature closely matched FSRs near 20 GHz. (b) Coupled rings pumped by a DFB laser that is self-injection locked to a resonator mode. Periodic pulse trains (light red arrow) are generated. Upper panel shows the cross-sectional waveguide geometry of the ring coupling region ($2.8 \mu\text{m}$ waveguide width and $2.4 \mu\text{m}$ waveguide gap). (c) Measured group velocity dispersion (GVD) parameter D_2 of the mode resonances versus wavelength. Zero dispersion is achieved near 1542 nm and 1559 nm. (d) Optical spectra of the generated frequency comb when pumped near the two zero-dispersion points. For the comb pumped at 1541 nm (gray), the span is 9.2 nm (as marked by the arrows). For the comb pumped at 1559 nm (orange), the span is 9.9 nm. The dashed line indicates the estimated on-chip line power of $1 \mu\text{W}$. (e) and (f) Measured microwave frequency spectrum of the detected microcomb output when pumped at 1542 nm (e) and 1560 nm (f). The resolution bandwidth is 10 kHz.

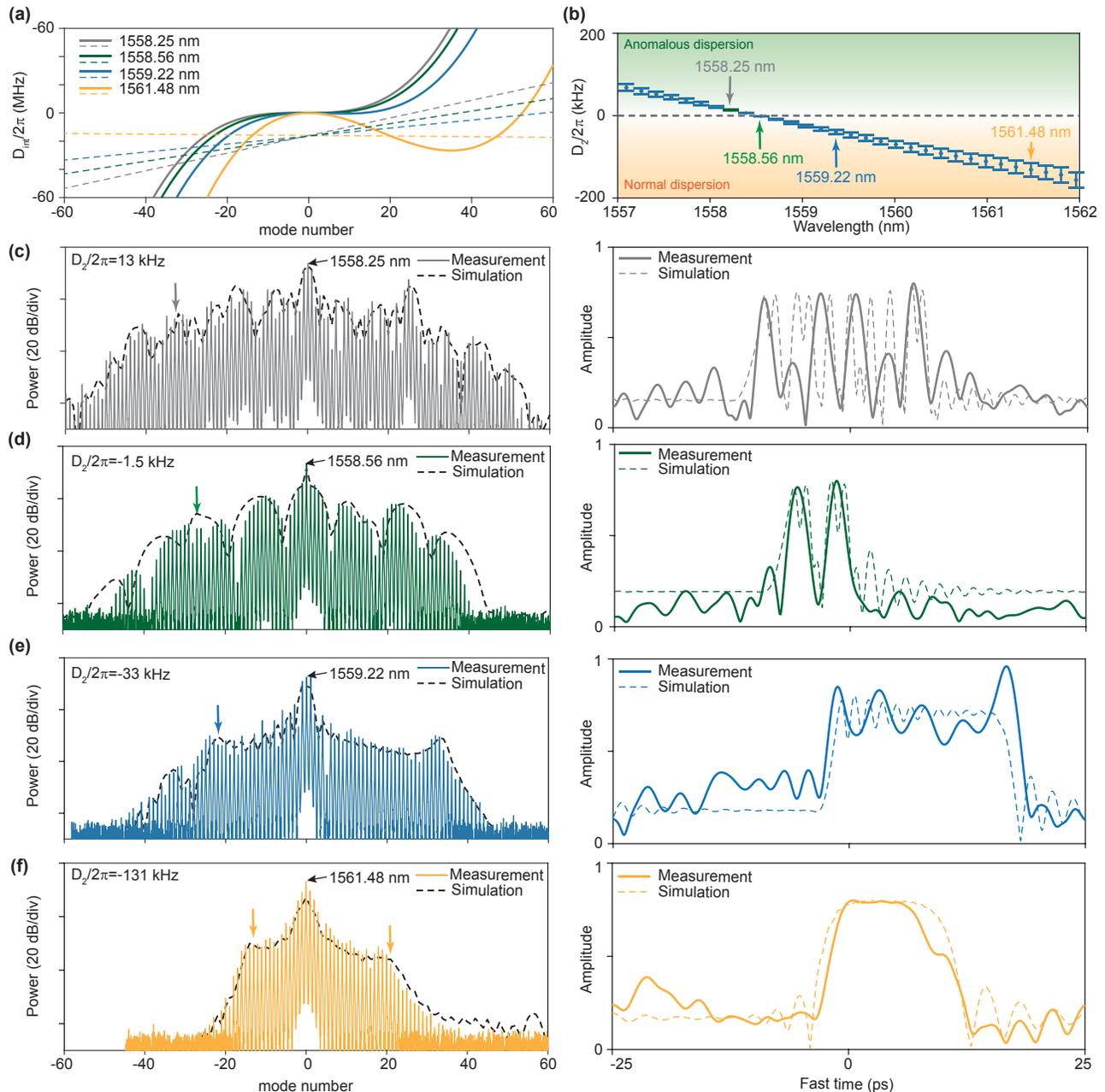


Fig. 2. Microcomb optical spectra and temporal waveforms measured at specific pumping wavelengths near the zero GVD wavelength. (a) Solid lines give the integrated dispersion, defined as $D_{\text{int}} = \omega_{\mu} - \omega_0 - D_1 \mu$ (right-hand side of Eq. 1), measured at the pumping wavelengths shown in the legend. The colored dashed lines denote the comb line frequencies (left-hand side of Eq. 1) when pumped at the specified pumping wavelengths. The intersection of the mode resonances (solid line) and comb lines (dashed line) generates a dispersive wave. (b) Measured GVD parameter D_2 versus wavelength near the zero GVD point. Arrows correspond to the pump wavelengths shown in (a). Error bar denotes standard deviation from the third-order polynomial fitting. (c–f) Left side: optical spectra of the microcomb when pumped near the zero-dispersion wavelength; the specific pumping wavelength is indicated and corresponds to values in (a). The simulated optical spectrum is plotted as the dashed black curve. The dispersive wave position from (a) is marked by arrows. Right side: measured microcomb temporal waveform during one round trip for the pumping wavelength given in the left panel.

(provided in the legend) near 1559 nm. In the plots, $\mu = 0$ corresponds to the pump line. The dispersion curves are measured using a radio frequency calibrated interferometer reference [10].

When pumped at near-zero dispersion, the comb spectral span is strongly influenced by comb radiation into a dispersive wave, which corresponds to the cavity modes that are nearly resonant with the comb lines. The mode number μ_{dw} of the dispersive wave is given as the solution to [32]

$$-\delta\omega + 2gP_0 + \delta\omega_{\text{rep}}\mu_{\text{dw}} = \frac{D_2}{2}\mu_{\text{dw}}^2 + \frac{D_3}{6}\mu_{\text{dw}}^3, \quad (1)$$

where $\delta\omega$ is the pump-laser cavity detuning as regulated by the self-injection feedback, g is Kerr nonlinear coefficient, P_0 is photon number of the pumped cavity resonance, $\delta\omega_{\text{rep}}$ is the difference between comb repetition rate and cavity free-spectral range (D_1), and D_2 and D_3 are second- and third-order dispersion parameters, respectively. Figure 2(b) gives the measured second-order

dispersion (D_2) parameter at these same pumping wavelengths, and $D_3 = 7.5$ kHz is used for all pumping wavelengths. The left side of Eq. (1) corresponds to the frequency comb lines and is plotted as the colored dashed lines in Fig. 2(a). In making these line plots, $\delta\omega$ and $\delta\omega_{\text{rep}}$ are numerically simulated (Supplement 1, Note 4). The right side of Eq. (1) is the integrated dispersion and fitted to the experimentally measured dispersion as noted above. At each pumping wavelength, the dispersive wave mode number μ_{dw} can be obtained as the intercept between the comb frequencies (dashed lines) and the corresponding integrated dispersion curve (solid lines).

The dispersive wave position is marked with an arrow in the left panels of Figs. 2(c)–2(f), which show the measured spectra for SIL pumping at the wavelengths in Fig. 2(a). The arrow position provides the trend of a measured comb span for the negative mode numbers. The overall comb spectral span tends to be determined by this dispersive wave. Note that in Fig. 2, the third dispersive wave (after mode number ~ 50) is absent in both the measured and simulated optical spectrum, which is a result of insufficient pump power. The comb spectrum in Fig. 2(e) also appears in Fig. 1(d). It spans 9.9 nm (1.22 THz) and features on-chip comb-line power higher than 1 μW , marked with arrows. This comb has superior spectral coverage compared to previous SIL operated normal GVD microcombs [7,19]. It also features an increased number of comb lines compared to higher repetition rate nonbright combs directly III-V pumped with optical isolation [33]. As also shown in Fig. 1(d), when pumped at 1541 nm near the other zero-dispersion wavelength, a microcomb spanning 9.2 nm (1.16 THz) is realized. These comb states both feature pump power conversion efficiency as high as 26% (see Supplement 1, Note 2).

4. IMAGING OF MODE-LOCKED MICROCOMB STATES

While the temporal envelope of pulses produced by normal GVD combs has been measured using cross-correlation [17], near-zero GVD operation allows access to a wider variety of comb states, including soliton molecules (bounded bright solitons) and switching waves [32,34]. These interesting states have been numerically analyzed [22,35,36], but they have so far not been observed in the time domain. This is the result of current zero-dispersion systems being generated at challenging high repetition rates or by using a pulsed pump in which case the comb waveform is influenced by the pump pulse waveform [23,37,38]. Here, the linear optical sampling technique assisted with an electro-optic frequency comb is implemented to image the temporal profile of the various comb states [18,27]. The sampling EO comb spans ~ 5 nm with 33 lines, corresponding to a ~ 1.5 ps pulse in the time domain, and its repetition rate is set to be slightly higher than the zero-dispersion microcomb. Note that the temporal duration of the soliton pulse [for example, 2.6 ps FWHM in Fig. 2(d) for the left pulse in measurement] is close to the pulse width of the EO-comb (~ 1.5 ps); thus, the imaging result may not perfectly resolve the fine structure in the temporal waveforms. By combining the EO comb and the generated comb at the “drop” port, and detecting with a fast photodetector, the sampled microcomb signal is recorded by an oscilloscope for processing.

Experimental results are presented in the right panels of Figs. 2(c)–2(f). At the anomalous side ($D_2 > 0$) of the near-zero GVD wavelength, the strong dispersive wave binds several solitons

into soliton clusters, as observed in the right panel of Fig. 2(c). The interference between the pulses creates the multiple fringes that are apparent in the optical spectrum shown in the left panel of Fig. 2(c). Numerical simulations in the time domain and frequency domain are also presented as dashed curves in Figs. 2(c)–2(f). The clustered soliton formation is preserved for near-vanishing GVD ($D_2/2\pi = -1.5$ kHz), as shown in Fig. 2(d), where a soliton dimer is imaged. The corresponding optical spectrum is shown in the left panel of Fig. 2(d). For the pumping wavelengths with normal dispersion, the resulting waveforms are often called switching waves or “platicons” [18,19]. Here, the waveform evolves toward a square pulse as the dispersion becomes more normal ($D_2 < 0$), as shown in the right panels of Figs. 2(e) and 2(f). The present results experimentally demonstrate the evolution of comb states in the near-zero GVD regime with different GVD signs, and are consistent with a previous numerical study [22].

Generally, the operation of the comb with a small amount of normal dispersion [e.g., the state in Fig. 2(e), pumped at 1559.2 nm] provides both good spectral coverage as well as a temporal and spectral waveform that is more regular in shape. Furthermore, the square pulse nature of these states, apparent in the right panels of Figs. 2(e)–2(f), offers an increased duty cycle, which boosts the comb power conversion efficiency. As a result, the microwave and optical performance of the comb state in Fig. 2(e) is further studied below.

5. DISCIPLINE OF THE COMB REPETITION RATE

Discipline of comb repetition rate to an external reference such as a clock is important in many comb applications [3]. Generally, the repetition rate of microcombs is regulated by the pump-laser cavity detuning $\delta\omega$ [39,40], via channels including dispersive wave recoil [39], Raman self-frequency shift [41], and inhomogeneous backscattering [18,42]. As a result, with laser cavity detuning $\delta\omega$ controlled by the applied current on the pumping DFB laser, a fast feedback loop can be used to stabilize the microcomb’s repetition rate.

In the experiment shown in Fig. 3(a), the microcomb’s repetition rate is detected at the resonator drop port by a fast photodetector and analyzed by a signal analyzer (R&S FSUP). Pumping is at 1559.22 nm. The detected repetition rate tone is simultaneously split by a directional coupler after electrical amplification and mixed with a local oscillator that serves as the reference (SMB100A, Rhode & Schwarz). The mixed-down signal is sent to a servo controller and fed back to the current supply (LDX-3620B with a DC-coupled modulation response bandwidth < 1 MHz, Newport Corp.) of the DFB laser to provide fine-tuning control of the pump-laser cavity detuning frequency. The gap distance between the bus waveguide facet and the DFB laser head is regulated by a closed loop piezo (PZT) with a built-in strain gauge displacement sensor (MAX311D, Thorlabs).

The measured phase noise of the detected repetition rate tone under open-loop and disciplined (locked) conditions is shown in Fig. 3(b). The phase noise of the microwave reference is shown in gray. The phase noise of the disciplined repetition rate follows that of the microwave reference within the feedback bandwidth of approximately 100 kHz, as defined by the offset frequency where a “bump” is observed in its frequency spectrum. The microwave spectra of the SIL and disciplined comb are plotted in inset of Fig. 3(b). The repetition rate could be tuned by 60 kHz through tuning of the microwave reference, as shown in Fig. 3(c).

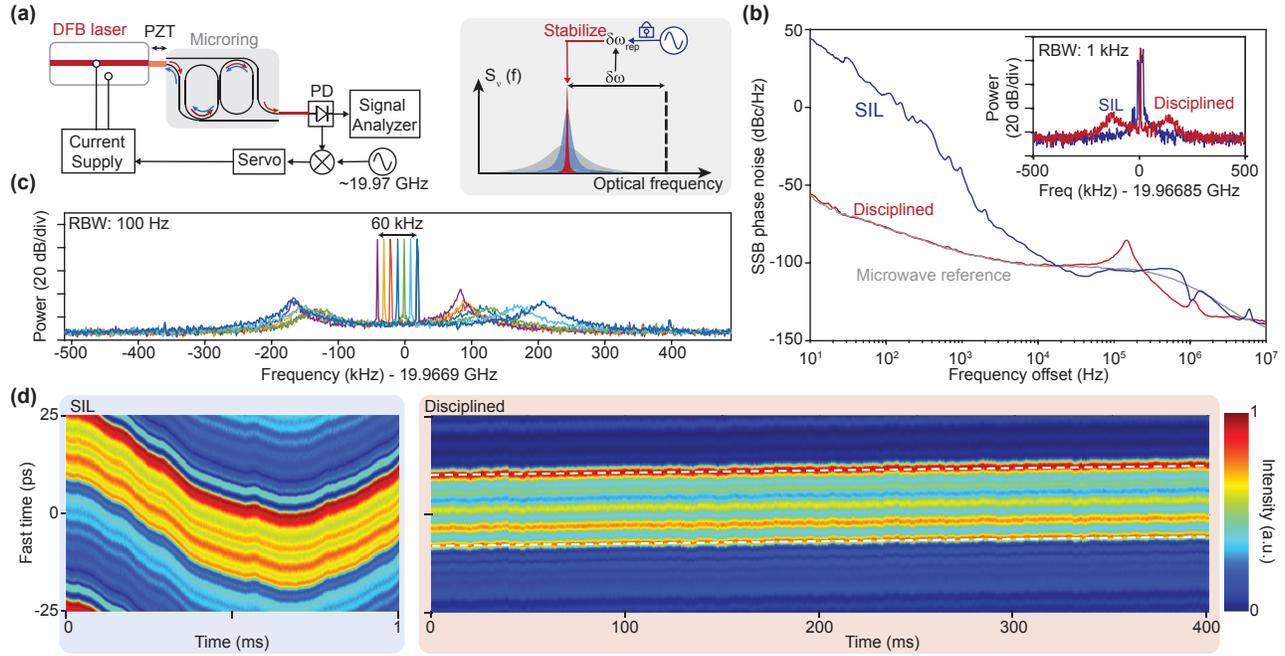


Fig. 3. Discipline of the SIL microcomb repetition rate to an external microwave reference. (a) Experimental setup for external disciplining of the SIL microcomb repetition rate. PZT, Piezo-electric transducer; PD, photodetector; and Servo, laser servo. Inset: Schematic view of laser detuning $\delta\omega$ stabilization via repetition rate discipline. Fluctuation in $\delta\omega$ leads to a fluctuation in the repetition rate $\delta\omega_{\text{rep}}$, which is measured and compared to a microwave reference to generate the error signal for feedback to the laser-driving current. Frequency noise of the free-running DFB laser (gray) is reduced by SIL (blue) and then reduced further by repetition rate locking (red). (b) Repetition rate phase noise and microwave spectra of the free-running SIL microcomb (blue) and the externally disciplined microcomb (red). Measured phase noise of the microwave reference is plotted in gray. (c) Repetition rate tuning of the external disciplined microcomb. Measured microwave tone of the comb is plotted in different colors. The resolution bandwidth is 100 Hz. (d) Stability of temporal waveform of the microcomb under free-running SIL (left) and external discipline (right). In the right panel, two dashed white lines give the linear motion of the waveform in the fast frame.

Disciplining the microcomb simultaneously stabilizes its temporal waveform. This is observable in Fig. 3(d), which shows the round-trip comb field plotted versus time. In the left panel, the data are presented under unlocked conditions and show the drift of the soliton waveform over a time scale of 1 ms. On the other hand, the disciplined microcomb features a measured soliton waveform that evolves very slowly and linearly (linear trend lines shown as white dashed lines). Here, the observable drift results from the difference in the sampling period between the oscilloscope and the EO sampling signal. All of the sampling data presented in Fig. 2 were obtained when the comb was externally disciplined.

6. COMB OFFSET FREQUENCY STABILIZATION UNDER REPETITION RATE DISCIPLINE

The pump laser frequency of the microcomb also determines the offset frequency of the microcomb. Self-injection locking of the pump laser here is known to improve the frequency stability [43]. In the present case, SIL stabilizes the DFB pump laser's frequency to the high- Q silicon nitride cavity mode and thereby stabilizes laser-cavity detuning $\delta\omega$ to a value that depends on the feedback phase and initial laser-cavity detuning without SIL feedback. The pump laser frequency noise under SIL and free-running operation is measured in Fig. 4. The measurement is performed by amplifying the microcomb output at the drop port using an erbium-doped fiber amplifier (EDFA) and filtering out the pump line with a waveshaper. The frequency noise of the line is then measured with a cross-correlation-based self-heterodyne measurement [44] within the measurement time of 400 ms. Compared to the free

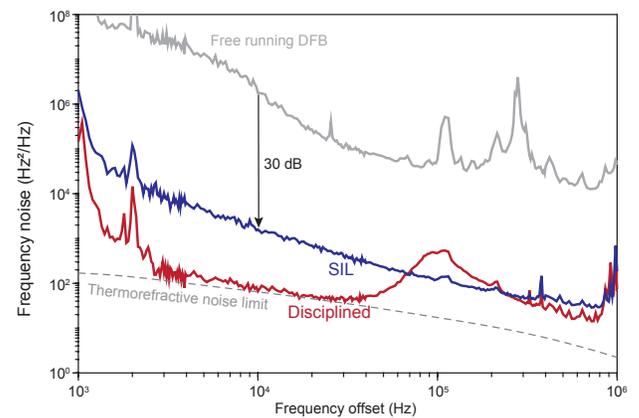


Fig. 4. Optical frequency noise of the pump laser (comb offset frequency). Gray curve gives the free-running (non-SIL) measurement, blue curve is for self-injection locked (SIL) operation, and the red curve is for repetition rate discipline using an external microwave reference. The thermorefractive noise floor is denoted by the dashed gray line.

running DFB laser (gray), the frequency noise of the pump laser is reduced by 30 dB under SIL operation (blue) at 10 kHz offset frequency. An integrated linewidth $\Delta\nu_c$ of 7.2 kHz is obtained ($\Delta\nu_c \equiv \int_{\Delta\nu_c}^{+\infty} S_{\delta\omega}(f)/f^2 df = \frac{1}{2\pi}$). The frequency noise here is still higher than the thermal noise limit given by the dashed gray curve in Fig. 4 [45] (see Supplement 1, Note 1).

Fluctuation of a microcomb's repetition rate $\delta\omega_{\text{rep}}$ is largely controlled by the pump laser-cavity detuning $\delta\omega$ [19,42]. As

schematically illustrated in the inset of Fig. 3(a), disciplining the microcomb's repetition rate thus simultaneously disciplines the laser pumping frequency relative to the pumped cavity resonance. With a fluctuation in $\delta\omega$ greatly reduced by disciplining the repetition rate, the frequency noise of the pump laser frequency (and comb offset frequency) is further stabilized to the thermorefractive noise limit, as plotted in red in Fig. 4. The bumps at 1 kHz and 2 kHz originate from the piezo-electric motor used to control the gap between the DFB laser head and the photonic chip. In principle, heterogeneous integration or butterfly packaging [6] of the pump and the resonator would eliminate the need for this servo control or at least replace it with a potentially faster equivalent control. It is noted that comb offset noise at lower offset frequencies than the measurement in Fig. 4 is generally possible from (but not limited to) the ambient, including temperature fluctuations and mechanical vibrations, other than the noise sources noted above [46]. With the same definition as above, the calculated integrated linewidth is 2.1 kHz, which is comparable to an external cavity diode laser pumped microcomb [47].

7. SUMMARY

We have demonstrated a microwave rate mode-locked microcomb with near-zero GVD using CMOS-ready CR resonators. The reduced GVD enables spectrally broader microcomb operation using integrated photonics with high conversion efficiency. Self-injection-locked operation of the microcomb provides for turnkey operation and optical linewidth reduction. A record number of comb lines is generated for nonamplified and non-pulse-pumped operation of a normal dispersion microcomb. The dispersion engineering scheme in this paper can be extended to other wavelengths and different photonic platforms. Disciplining the microcomb to an external microwave reference simultaneously stabilizes its microwave tone, temporal waveform, and optical frequency. The external discipline for the hybrid-integrated microcomb source demonstrated here can be used in a two-point optical frequency division system [26] for low-noise microwave synthesis.

Note added in proof: A study of the anomalous dispersion regime in this coupled resonator system is reported in [48].

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Data availability. Data underlying the results presented in this paper are not publicly available at this time but may be obtained from the authors upon reasonable request.

Supplemental document. See Supplement 1 for supporting content.

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REFERENCES

1. K. J. Vahala, "Optical microcavities," *Nature* **424**, 839–846 (2003).

2. T. J. Kippenberg, A. L. Gaeta, M. Lipson, and M. L. Gorodetsky, "Dissipative Kerr solitons in optical microresonators," *Science* **361**, eaan8083 (2018).
3. S. A. Diddams, K. Vahala, and T. Udem, "Optical frequency combs: coherently uniting the electromagnetic spectrum," *Science* **369**, eaay3676 (2020).
4. L. Chang, S. Liu, and J. E. Bowers, "Integrated optical frequency comb technologies," *Nat. Photonics* **16**, 95–108 (2022).
5. B. Stern, X. Ji, Y. Okawachi, A. L. Gaeta, and M. Lipson, "Battery-operated integrated frequency comb generator," *Nature* **562**, 401–405 (2018).
6. B. Shen, L. Chang, J. Liu, *et al.*, "Integrated turnkey soliton microcombs," *Nature* **582**, 365–369 (2020).
7. W. Jin, Q.-F. Yang, L. Chang, *et al.*, "Hertz-linewidth semiconductor lasers using CMOS-ready ultra-high-Q microresonators," *Nat. Photonics* **15**, 346–353 (2021).
8. C. Xiang, J. Liu, J. Guo, *et al.*, "Laser soliton microcombs heterogeneously integrated on silicon," *Science* **373**, 99–103 (2021).
9. T. Herr, V. Brasch, J. Jost, I. Mirgorodskiy, G. Lihachev, M. Gorodetsky, and T. Kippenberg, "Mode spectrum and temporal soliton formation in optical microresonators," *Phys. Rev. Lett.* **113**, 123901 (2014).
10. X. Yi, Q.-F. Yang, K. Y. Yang, M.-G. Suh, and K. Vahala, "Soliton frequency comb at microwave rates in a high-Q silica microresonator," *Optica* **2**, 1078–1085 (2015).
11. W. Liang, D. Elyahu, V. Ilchenko, A. Savchenkov, A. Matsko, D. Seidel, and L. Maleki, "High spectral purity Kerr frequency comb radio frequency photonic oscillator," *Nat. Commun.* **6**, 7957 (2015).
12. M.-G. Suh and K. Vahala, "Gigahertz-repetition-rate soliton microcombs," *Optica* **5**, 65–66 (2018).
13. K. Y. Yang, D. Y. Oh, S. H. Lee, Q.-F. Yang, X. Yi, B. Shen, H. Wang, and K. Vahala, "Bridging ultrahigh-Q devices and photonic circuits," *Nat. Photonics* **12**, 297 (2018).
14. J. Liu, E. Lucas, A. S. Raja, J. He, J. Riemensberger, R. N. Wang, M. Karpov, H. Guo, R. Bouchand, and T. J. Kippenberg, "Photonic microwave generation in the X- and K-band using integrated soliton microcombs," *Nat. Photonics* **14**, 486–491 (2020).
15. N. Kondratiev, V. Lobanov, A. Cherenkov, A. Voloshin, N. Pavlov, S. Koptyaev, and M. Gorodetsky, "Self-injection locking of a laser diode to a high-Q WGM microresonator," *Opt. Express* **25**, 28167–28178 (2017).
16. N. Pavlov, G. Lihachev, S. Koptyaev, E. Lucas, M. Karpov, N. Kondratiev, I. Bilenko, T. Kippenberg, and M. Gorodetsky, "Soliton dual frequency combs in crystalline microresonators," *Opt. Lett.* **42**, 514–517 (2017).
17. X. Xue, Y. Xuan, Y. Liu, P.-H. Wang, S. Chen, J. Wang, D. E. Leaird, M. Qi, and A. M. Weiner, "Mode-locked dark pulse Kerr combs in normal-dispersion microresonators," *Nat. Photonics* **9**, 594–600 (2015).
18. H. Wang, B. Shen, Y. Yu, Z. Yuan, C. Bao, W. Jin, L. Chang, M. A. Leal, A. Feshali, M. Paniccia, J. E. Bowers, and K. Vahala, "Self-regulating soliton switching waves in microresonators," *Phys. Rev. A* **106**, 053508 (2022).
19. G. Lihachev, W. Weng, J. Liu, L. Chang, J. Guo, J. He, R. N. Wang, M. H. Anderson, Y. Liu, J. E. Bowers, and T. J. Kippenberg, "Platicon microcomb generation using laser self-injection locking," *Nat. Commun.* **13**, 1771 (2022).
20. A. Fülöp, M. Mazur, A. Lorences-Riesgo, Ó. B. Helgason, P.-H. Wang, Y. Xuan, D. E. Leaird, M. Qi, P. A. Andrekson, A. M. Weiner, and V. Torres-Company, "High-order coherent communications using mode-locked dark-pulse Kerr combs from microresonators," *Nat. Commun.* **9**, 1598 (2018).
21. C. Xiang, W. Jin, and J. E. Bowers, "Silicon nitride passive and active photonic integrated circuits: trends and prospects," *Photon. Res.* **10**, A82–A96 (2022).
22. M. H. Anderson, W. Weng, G. Lihachev, A. Tikan, J. Liu, and T. J. Kippenberg, "Zero dispersion Kerr solitons in optical microresonators," *Nat. Commun.* **13**, 4764 (2022).
23. S. Zhang, T. Bi, and P. Del'Haye, "Microresonator soliton frequency combs in the zero-dispersion regime," arXiv, arXiv:2204.02383 (2022).
24. Z. Li, Y. Xu, C. Todd, G. Xu, S. Coen, S. G. Murdoch, and M. Erkintalo, "Observations of existence and instability dynamics of near-zero-dispersion temporal Kerr cavity solitons," *Phys. Rev. Res.* **3**, 043207 (2021).
25. S. B. Papp, K. Beha, P. Del'Haye, F. Quinlan, H. Lee, K. J. Vahala, and S. A. Diddams, "Microresonator frequency comb optical clock," *Optica* **1**, 10–14 (2014).

26. J. Li, X. Yi, H. Lee, S. A. Diddams, and K. J. Vahala, "Electro-optical frequency division and stable microwave synthesis," *Science* **345**, 309–313 (2014).
27. X. Yi, Q.-F. Yang, K. Y. Yang, and K. Vahala, "Imaging soliton dynamics in optical microcavities," *Nat. Commun.* **9**, 3565 (2018).
28. R. Boeck, N. A. Jaeger, N. Rouger, and L. Chrostowski, "Series-coupled silicon racetrack resonators and the vernier effect: theory and measurement," *Opt. Express* **18**, 25151–25157 (2010).
29. M. Soltani, A. Matsko, and L. Maleki, "Enabling arbitrary wavelength frequency combs on chip," *Laser Photon. Rev.* **10**, 158–162 (2016).
30. S. Kim, K. Han, C. Wang, J. A. Jaramillo-Villegas, X. Xue, C. Bao, Y. Xuan, D. E. Leaird, A. M. Weiner, and M. Qi, "Dispersion engineering and frequency comb generation in thin silicon nitride concentric microresonators," *Nat. Commun.* **8**, 372 (2017).
31. Ó. B. Helgason, F. R. Arteaga-Sierra, Z. Ye, K. Twayana, P. A. Andrekson, M. Karlsson, J. Schröder, and V. Torres-Company, "Dissipative solitons in photonic molecules," *Nat. Photonics* **15**, 305–310 (2021).
32. Z. Li, Y. Xu, S. Coen, S. G. Murdoch, and M. Erkintalo, "Experimental observations of bright dissipative cavity solitons and their collapsed snaking in a Kerr resonator with normal dispersion driving," *Optica* **7**, 1195–1203 (2020).
33. H. Shu, L. Chang, C. Lao, B. Shen, W. Xie, X. Zhang, M. Jin, Y. Tao, R. Chen, Z. Tao, S. Yu, Q.-F. Yang, X. Wang, and J. E. Bowers, "Sub-milliwatt, widely-tunable coherent microcomb generation with feedback-free operation," *arXiv*, arXiv:2112.08904 (2021).
34. B. Garbin, Y. Wang, S. G. Murdoch, G.-L. Oppo, S. Coen, and M. Erkintalo, "Experimental and numerical investigations of switching wave dynamics in a normally dispersive fibre ring resonator," *Eur. Phys. J. D* **71**, 1–8 (2017).
35. P. Parra-Rivas, D. Gomila, F. Leo, S. Coen, and L. Gelens, "Third-order chromatic dispersion stabilizes Kerr frequency combs," *Opt. Lett.* **39**, 2971–2974 (2014).
36. P. Parra-Rivas, D. Gomila, and L. Gelens, "Coexistence of stable dark- and bright-soliton Kerr combs in normal-dispersion resonators," *Phys. Rev. A* **95**, 053863 (2017).
37. M. H. Anderson, F. Leo, M. J. Erkintalo, S. Coen, and S. G. Murdoch, "Measurement of the Raman self-frequency shift of a temporal cavity soliton," in *Photonics and Fiber Technology 2016 (ACOFT, BGPP, NP)*, OSA Technical Digest (online) (Optica Publishing Group, 2016), paper NW4A.4.
38. Z. Xiao, T. Li, M. Cai, H. Zhang, Y. Huang, K. Wu, and J. Chen, "Zero-dispersion soliton generation in a high-Q fiber Fabry-Pérot microresonator," in *Conference on Lasers and Electro-Optics*, J. Kang, S. Tomasulo, I. Ilev, D. Müller, N. Litchinitser, S. Polyakov, V. Podolskiy, J. Nunn, C. Dorrer, T. Fortier, Q. Gan, and C. Saraceno, eds., OSA Technical Digest (Optica Publishing Group, 2021), paper SW2H.6.
39. X. Yi, Q.-F. Yang, X. Zhang, K. Y. Yang, X. Li, and K. Vahala, "Single-mode dispersive waves and soliton microcomb dynamics," *Nat. Commun.* **8**, 14869 (2017).
40. E. Lucas, P. Brochard, R. Bouchand, S. Schilt, T. Südmeyer, and T. J. Kippenberg, "Ultralow-noise photonic microwave synthesis using a soliton microcomb-based transfer oscillator," *Nat. Commun.* **11**, 374 (2020).
41. X. Yi, Q.-F. Yang, K. Y. Yang, and K. Vahala, "Theory and measurement of the soliton self-frequency shift and efficiency in optical microcavities," *Opt. Lett.* **41**, 3419–3422 (2016).
42. N. M. Kondratiev, V. E. Lobanov, E. A. Lonshakov, N. Y. Dmitriev, A. S. Voloshin, and I. A. Bilenko, "Numerical study of solitonic pulse generation in the self-injection locking regime at normal and anomalous group velocity dispersion," *Opt. Express* **28**, 38892–38906 (2020).
43. W. Liang, V. Ilchenko, A. Savchenkov, A. Matsko, D. Seidel, and L. Maleki, "Whispering-gallery-mode-resonator-based ultranarrow linewidth external-cavity semiconductor laser," *Opt. Lett.* **35**, 2822–2824 (2010).
44. Z. Yuan, H. Wang, P. Liu, B. Li, B. Shen, M. Gao, L. Chang, W. Jin, A. Feshali, M. Paniccia, J. E. Bowers, and K. Vahala, "Correlated self-heterodyne method for ultra-low-noise laser linewidth measurements," *Opt. Express* **30**, 25147–25161 (2022).
45. N. Kondratiev and M. Gorodetsky, "Thermorefractive noise in whispering gallery mode microresonators: analytical results and numerical simulation," *Phys. Lett. A* **382**, 2265–2268 (2018).
46. N. R. Newbury and W. C. Swann, "Low-noise fiber-laser frequency combs," *J. Opt. Soc. Am. B* **24**, 1756–1770 (2007).
47. F. Lei, Z. Ye, Ó. B. Helgason, A. Fülöp, M. Girardi, and V. Torres-Company, "Optical linewidth of soliton microcombs," *Nat. Commun.* **13**, 3161 (2022).
48. Z. Yuan, M. Gao, Y. Yu, H. Wang, W. Jin, Q.-X. Ji, A. Feshali, M. Paniccia, J. Bowers, and K. Vahala, "Soliton pulse pairs at multiple colors in normal dispersion microresonators," *arXiv*, arXiv:2301.10976 (2023).